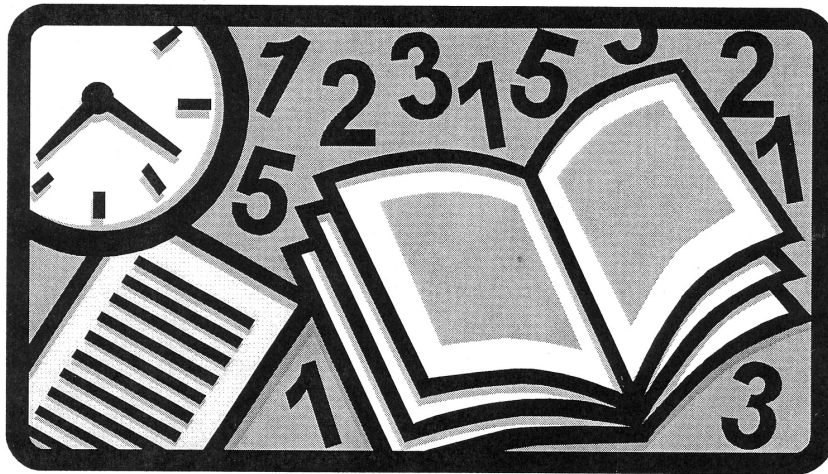


SUMMER MATH PACKET  
FOR STUDENTS COMPLETING  
ALGEBRA 1 – GRADE 8  
ALGEBRA 1  
ESSENTIALS OF ALGEBRA 1 – B



NAME: \_\_\_\_\_

TEACHER: \_\_\_\_\_

DATE COMPLETED: \_\_\_\_\_

**DIRECTIONS:** Complete each problem, **showing all work in the space provided below** it. You **MUST** show work, or explain your solution in order to receive credit for the answer. There are hints for each problem in the right hand margin of the page.

**QUESTION**

**HINT**

1. If  $4x + 35 = 49.8$ , then  $7x =$

1. Solve for  $x$ , then find  $7x$

2. After a 15% discount, a pair of running shoes costs \$102.00. How much were the shoes before the discount was taken?

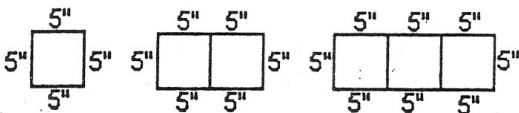
2. If there was a 15% discount, what was the % paid? Write an equation to solve.

3. If 40% of some number is 34, what is 68% of that same number?

3. Remember  $\frac{P}{100} (N) = R$

4. If you lined up 20 squares in a row with each side equal to 5 inches, what would the perimeter measure?

4. Use the squares in the diagram to find a pattern with the number of squares and the number of sides to predict the perimeter.



## QUESTION

5. Consider the following pattern in which to exponents are integers:

$$0^0, 1^1, 2^2, 3^3, \dots$$

What is the value of the seventh term in this pattern?

- A. 3, 125
- B. 46,656
- C. 279,936
- D. 823,543

6. Bardoll's Market sells pecans at \$4.95 for a ten ounce bag. At this rate, the cost of one pound of pecans would be between

- A. \$6.90 and \$7.00
- B. \$7.90 and \$8.00
- C. \$8.90 and \$9.00
- D. \$9.90 and \$10.00

7. What is the rate of 66 feet per second expressed as miles per hour?

- A. 43 mph
- B. 44 mph
- C. 45 mph
- D. 46 mph

8. How many different three letter words can be made out of the letters of the word LEARN (not all of the words have to make sense)?

- A. 6
- B. 60
- C. 90
- D. 120

## HINT

5. Think about what the seventh term would look like, then calculate it on your calculator.

6. Find the cost of 1 ounce of pecans. Remember that there are 16 ounces in one pound.

7.  $5280 \text{ feet} = 1 \text{ mile}$   
 $3600 \text{ seconds} = 1 \text{ hour}$

8. How many possible letters could you use for the first letter of the "word"? How many possible letters could you use for the second letter? How many for the third letter?

## QUESTION

9. The numbers 1 to 100 are written on index cards and placed in a box. After the box is thoroughly shaken, Fred, who is blindfolded, picks an index card.

A. What is the probability that the number drawn is greater than 65?

B. Out of the same 100 index cards, what is the probability that the number drawn is divisible by 3?

10. Thirty slips of paper, numbered 1 to 30, are placed in a box. What is the probability of picking a slip of paper with a number that has a 4 as one of the digits?

11. In drawing the plans for a house, the architect makes a scale drawing where  $\frac{1}{8}$  inch = 1 foot. If the actual dimensions of a room are to be 15 feet by 30 feet, what are the scale dimensions?

- A. 1.625 inches by 3.25 inches
- B. 1.875 inches by 3.75 inches
- C. 2 inches by 4 inches
- D. 2.125 inches by 4.25 inches

12. One cubic foot will hold 7.5 gallons of water. If Geraldo's waterbed mattress measures 7 feet by 6 feet by 6 inches, how many gallons of water will he need to fill the mattress?

## HINT

9. The probability that something is likely to occur =

$\frac{\text{number of outcomes in the event}}{\text{number of outcomes in the sample space}}$

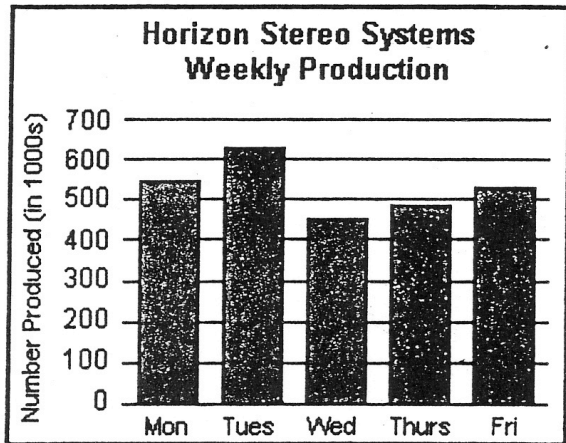
10. Look at #9

11. Set up a proportion for each dimension, comparing the size in the scale drawing to the size in the room.

12. Volume = length X width X height

13. The chart shows Horizon Stereo Systems' weekly production. The approximate per cent of decrease in stereo production on Thursday as compared to Tuesday is between

- A. 19% and 25%
- B. 30% and 37%
- C. 39% and 45%
- D. 48% and 56%



14. What is the missing value in the table below?

x	0.5	1	1.5	2	2.5	...	37.5
y	0.75	1.5	2.25	3	3.75	...	?

15. For this list of scores:

125, 136, 127, 142, 151, 127, 136, 127, 200, 214, 145

determine

- A. the mean \_\_\_\_\_
- B. the range \_\_\_\_\_
- C. the mode \_\_\_\_\_
- D. the median \_\_\_\_\_

If a score of 220 were added to the list, determine the new values for each.

13. Percent of increase or decrease is given by the formula:

$$\frac{\text{Change in value}}{\text{Original value}} \times 100$$

Find a relationship between x and y for the other pairs, and use that to find the missing value.

15. Mean is the average

Range is the difference from the highest to lowest score

Mode is the most frequent score

Median is the middle score, if they are arranged in order. If there is an even number of scores, it is the average of the two middle scores.

## QUESTION

16. Pierre wants to order a T-shirt with "Pierre" printed on it. The T-shirt costs \$7.99. There is a charge of \$.59 for each letter printed on it. Find the total cost, including a 6% sales tax. (Round the final answer up to the nearest cent)

- A. \$3.76
- B. \$11.53
- C. \$9.10
- D. \$12.22

17. Consider the following three statements:

- I. Every year we spend \$5 million on exercise programs and \$20 million on hot dogs.
- II. Every year we spend  $\frac{1}{5}$  as much on exercise programs as we do on hot dogs.
- III. Every year we spend  $\frac{1}{4}$  as much on exercise programs as we do on hot dogs.

Which statements above are equivalents to each other?

- A. I and II only
- B. I and III only
- C. II and III only
- D. I, II, and III

18. Howard works in an electronics store. For every item he sells, he earns a 10% commission. If Howard sold the following items, how much total commission would he earn?

computer \$2790  
2 packs of disks \$12.50  
camera \$420

## HINT

16. Calculate the total cost of the T-shirt and all letters. Then calculate the sales tax on that total. Remember that 6% is .06

17. Set up a ratio of exercise to hot dogs to see which statements are equivalent.

18. Calculate the Howard's total sales, then find 10% of that total. Remember the formula

$$\frac{P}{100} (N) = R$$

## QUESTION

19. Coco and Mariko went to the count fair together. They brought \$50 in all. Coco brought \$8 less than Mariko. How much money did Mariko bring?

- A. between \$1 and \$10
- B. between \$10 and \$20
- C. between \$20 and \$30
- D. between \$30 and \$40

20. An old fashioned 45 rpm vinyl record revolves on a turntable 45 times each minute. How long does it take for a record to revolve once on its turntable?

- A. .75 second
- B. 1 second
- C. 1.25 seconds
- D. 1.33 seconds

21. At \$12 an hour, how much does Kirsten earn in one week if she works the following hours:

Monday - 9 AM to 3 PM  
Tuesday - 9:30 AM to 4:30 PM  
Wednesday - 10 AM to 12 NOON  
Thursday - 11 AM to 5 PM  
Friday - 10:30 AM to 3 PM

Kirsten has one hour for lunch (12 NOON to 1 PM) She is not paid for this hour.

- A. \$246
- B. \$252.50
- C. \$258
- D. \$318

## HINT

19. Write an equation to represent this situation. Let  $x$  represent the amount of money Mariko brought. Write an expression for the amount of money Coco brought, then write an equation and solve.

20. Use equivalent statements to solve this:

45 times in 1 minute  
1 time in \_\_\_ minute

21. Calculate the total time she worked each day, remember to subtract the time for lunch. Then multiply that total by the amount she makes each hour to find the total she made.

## QUESTION

22. Max Lee, a stockbroker, earns a salary of \$1660.98, plus a commission of 3% of the value of the stocks he buys and sells for his clients. He sold 100 shares of stock priced at \$22.69 per share. How much commission will Mr. Lee earn?

23. On Monday, Lena ran a 440-yard race in 1 minute, 20 seconds. On Friday, she ran a 100-yard race in 15 seconds. On which day's race did Lena run at a faster average speed, and what was her average speed during that race?

- A. Monday, 16.5 feet per second
- B. Monday, 11 feet per second
- C. Friday, 20 feet per second
- D. Friday, 25 feet per second

24. What is the next term in the following sequence?

10, 11, 14, 19, 26,...

- A. 32
- B. 33
- C. 34
- D. 35

25. In  $m/3 = 60$ , what is the value of  $3m$ ?

## HINT

22. Calculate the total price of the stock. Use that to calculate the commission.

23. Find her speed in yards per second, then compare which is faster and by how much.

24. Look for a pattern to get from one term to the next. If you are not adding or multiplying by the same number each time, look for a pattern

25. Solve for  $m$ , then find  $3m$



# HIGH SCHOOL PROFICIENCY ASSESSMENT MATHEMATICS REFERENCE SHEET

*Use the information below, as needed, to answer questions on the Mathematics Section of the High School Proficiency Assessment.*

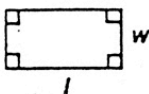
$$\pi = 3.14 \text{ or } \frac{22}{7}$$

Circle



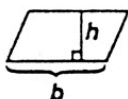
Area =  $\pi r^2$   
Circumference =  $2\pi r$

Rectangle



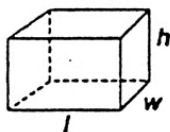
Area =  $lw$   
Perimeter =  $2(l + w)$

Parallelogram



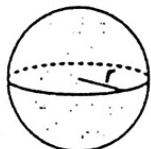
Area =  $bh$

Rectangular Prism



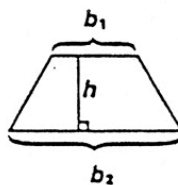
Volume =  $lwh$   
Surface Area =  $2lw + 2wh + 2lh$

Sphere



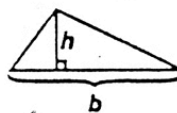
Volume =  $\frac{4}{3}\pi r^3$

Trapezoid



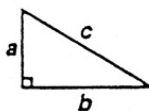
Area =  $\frac{1}{2}(b_1 + b_2)h$

Triangle



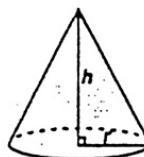
Area =  $\frac{1}{2}bh$

Pythagorean Formula



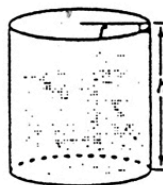
$c^2 = a^2 + b^2$

Cone



Volume =  $\frac{1}{3}\pi r^2 h$

Cylinder



Volume =  $\pi r^2 h$

*Use the following equivalents for your calculations.*

12 inches = 1 foot  
3 feet = 1 yard  
36 inches = 1 yard  
5,280 feet = 1 mile  
1,760 yards = 1 mile

100 centimeters = 1 meter  
1000 meters = 1 kilometer

1000 milliliters (mL) =  
1 liter (L)

60 seconds = 1 minute  
60 minutes = 1 hour  
24 hours = 1 day  
7 days = 1 week  
52 weeks = 1 year

1000 watt hours =  
1 kilowatt hour

1000 milligrams = 1 gram  
100 centigrams = 1 gram  
10 grams = 1 dekagram  
1000 grams = 1 kilogram

8 fluid ounces = 1 cup  
2 cups = 1 pint  
2 pints = 1 quart  
4 quarts = 1 gallon

The sum of the measures of the interior angles of a triangle =  $180^\circ$

The measure of a circle is  $360^\circ$  or  $2\pi$  radians

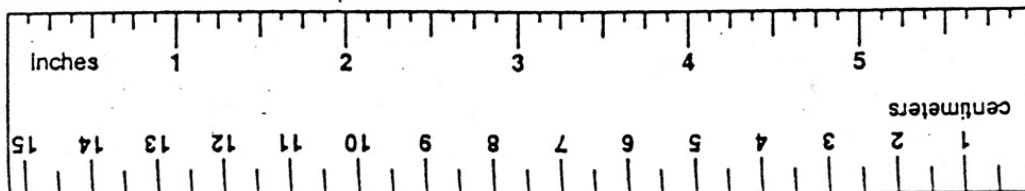
Distance = rate  $\cdot$  time    Interest = principal  $\cdot$  rate  $\cdot$  time

Compound Interest Formula:  $A = p \left(1 + \frac{r}{k}\right)^{kt}$

$A$  = amount after  $t$  years;  $p$  = principal;  $r$  = annual interest rate;  $t$  = number of years;  
 $k$  = number of times compounded per year

The number of combinations of  $n$  elements taken  $r$  at a time is given by  $\frac{n!}{(n-r)!r!}$

The number of permutations of  $n$  elements taken  $r$  at a time is given by  $\frac{n!}{(n-r)!}$



## REFERENCES FOR SUMMER MATH PACKET

If you have questions about any of the problems on the Summer Math Packet, here are some useful references.

### 1. EMAIL:

[summermath@rutherfordschools.org](mailto:summermath@rutherfordschools.org)

You can email the math department and someone will respond with assistance. Please be specific as to which packet and problem number you are doing.

### 2. HERE ARE SOME ADDITIONAL HELPFUL WEBSITES:

- a. On this site you can search for help with particular topics in Algebra.

[www.purplemath.com](http://www.purplemath.com)

- b. This site has a scientific calculator you can use

[www.lanl.gov/projects/cctc/resources/tools/calculator.html](http://www.lanl.gov/projects/cctc/resources/tools/calculator.html)

- c. At the Dr. Math site, you can email them a question, or search for a particular question

<http://mathforum.org/dr.math/>

- d. Here you can post a question, and get a reply also:

<http://www.webcalc.net>